

Figure 1. Atom and torsion-angle numbering in acetylcholine.


1


II

Figure 2. Suggested rotamers for the $\mathrm{C}(6)-\mathrm{O}(1)-\mathrm{C}(5)-\mathrm{C}(4)$ fragment. Rotamer I: $\tau_{1} \sim 90^{\circ}$, rotamer II: $\tau_{1} \sim 180^{\circ}$.

Table I. Acetylcholine: ${ }^{3} J_{13} \mathrm{C}(6)-\mathrm{O}(1)-\mathrm{C}(5)-\mathrm{H}$ Values, ${ }^{a}$ Fractional Rotamer Populations, and $\Delta G^{\circ}$ Values at Different Temperatures for the Fragment $C(6)-O(1)-C(5)-C(4)$

| temp, ${ }^{\circ} \mathrm{C}$ | ${ }^{3} J_{13} \mathrm{COCH}, \mathrm{Hz}$ | fractional <br> rotamer population |  | $\Delta G^{\circ}$, <br> $\mathrm{cal} / \mathrm{mol}$ |
| :---: | :---: | :---: | :---: | :---: |
| 10 | 2.55 | $N_{\mathrm{I}}$ | $N_{\mathrm{II}}$ | 0.312 |
| 30 | 2.66 | 0.335 | 0.688 | -443 |
| 50 | 2.78 | 0.360 | 0.640 | -412 |
| 70 | 2.85 | 0.375 | 0.625 | -368 |

${ }^{a} \pm 0.05 \mathrm{~Hz}$. Consequently the rotamer populations $N$ and $\Delta G^{\circ}$ values are accurate to $\pm 0.010$ and $\pm 29 \mathrm{cal} / \mathrm{mol}$, respectively.
occurrence of a conformational equilibrium between different rotamers.

The rotational isomerism of ACh cation in solution can be represented by an equilibrium of the two rotamers shown in Figure 2 on the following grounds. First, torsion angles $\mathrm{C}(6)-\mathrm{O}(1)-\mathrm{C}-$ (5)-C(4) found in crystal structure of choline esters cluster round two values: 90 and $180^{\circ}$, except for two carbamoylcholine ions. ${ }^{3}$ Second, formate and acetate esters of ethyl alcohol show a nearly identical value of ${ }^{3}{ }^{13} \mathrm{Coch}$ ( 3.32 and 3.23 Hz , respectively ${ }^{10.11}$ ), thus suggesting that their conformational behavior is very similar. There is evidence derived from microwave spectroscopy ${ }^{12}$ that ethyl formate exists in solution as a mixture of one trans and two distorted gauche rotamers, the relative $\mathrm{C}-\mathrm{O}-\mathrm{C}-\mathrm{C}$ dihedral angles being approximately 85,180 , and $275^{\circ}$. Therefore, it seems reasonable to assume that, on rotation about the $\mathrm{C}-\mathrm{O}$ axis, the energy of the ACh cation goes through two minima occurring at nearly 90 and $180^{\circ}$. The rotamer with $\tau_{1} \sim 275^{\circ}$ seems highly implausible, keeping the fragment $\mathrm{O}(1)-\mathrm{C}(5)-\mathrm{C}(4)-\mathrm{N}$ in its more stable conformation $\left(\tau_{2} \simeq 60^{\circ}\right)^{7,8}$ due to the steric requirements of the $\mathrm{C}=\mathrm{O}$ and $\mathrm{N}\left(\mathrm{CH}_{3}\right)_{3}$ groups. Since the internal rotation is sufficiently rapid, the observed ${ }^{3} J_{13}$ coch value is a weighted average of the corresponding constants for the individual rotamers:

$$
\begin{align*}
& { }^{3} J_{13} \text { COCH }= \\
& N_{\mathrm{I}}^{1 / 2}\left[{ }^{3} \mathrm{~J}_{13}{ }_{\mathrm{COCH}}\left(30^{\circ}\right)+{ }^{3} J_{13} \mathrm{COCH}\left(150^{\circ}\right)\right]+N_{\mathrm{II}}{ }^{3} \mathrm{~J}^{13}{ }_{\mathrm{COCH}}\left(60^{\circ}\right) \tag{1}
\end{align*}
$$

where $N_{\mathrm{I}}$ and $N_{\mathrm{II}}$ are the fractional populations of rotamer I and II, respectively:

$$
\begin{equation*}
N_{\mathrm{I}}+N_{\mathrm{II}}=1 \tag{2}
\end{equation*}
$$

[^0]The coupling constant in rotamer I is given by the mean value $1 / 2\left[{ }^{3} J_{{ }^{13}}{ }_{\mathrm{coch}}\left(30^{\circ}\right)+{ }^{3} J_{13}{ }_{\mathrm{COCH}}\left(150^{\circ}\right)\right]$, owing to the rapid interconversion of rotamer I with its mirror image.
 be obtained from a Karplus-type relationship:

$$
\begin{equation*}
{ }^{3} J_{13^{3}, H}=A \cos ^{2} \varphi+B \cos \varphi+C \tag{3}
\end{equation*}
$$

Such a relationship has received experimental ${ }^{13-17}$ as well as theoretical ${ }^{18}$ evidence. However, reported ${ }^{3}{ }^{3}{ }_{13} \mathrm{CH}$ values exhibit a considerable scattering which has been attributed to structural parameters ${ }^{14,17}$ (e.g., carbon hybridization, electronegative substituents, nuclei sequence in the coupling pattern). The coefficients $A, B$, and $C$ for the ${ }^{3} J_{13}{ }^{\mathrm{cH}}$ coupling transmitted via the specific nuclei sequence ${ }^{13} \mathrm{C}-\mathrm{O}-\mathrm{C}-\mathrm{H}$ have been determined as follows. $C$ is considered to be negligible, as a survey of the literature shows that when $\varphi$ approaches $90^{\circ},{ }^{3} J_{13}$ cH becomes undetectable. ${ }^{14,15}$ The $A$ value ( 7.8 Hz ) is derived from averaged ${ }^{3} \mathrm{~J}_{13} \mathrm{COCH}$ couplings in methyl acetate ${ }^{10,11}$ and formate. ${ }^{10}$ Knowledge of $A$ and $C$ enables us to obtain $B$. A mean $B$ value of -1.8 Hz is computed from the values of vicinal ${ }^{13} \mathrm{C}, \mathrm{H}$ coupling constants ( 8.7 and 9.3 Hz ) measured in nearly trans and trans arrangements ( $\varphi=158$ and $180^{\circ}$ ) of the ${ }^{13} \mathrm{C}(0)-\mathrm{O}-\mathrm{C}-\mathrm{H}$ fragment in $2,5^{\prime}$-anhydro- $2^{\prime}, 3^{\prime}$-isopropylideneuridine ${ }^{16}$ and vinylene carbonate, ${ }^{19}$ respectively. When eq $1-3$ and the $\left.\left.{ }^{3} J_{13}{ }^{3}(6)-\alpha(1)-\mathrm{C}_{3}\right)+\mathrm{t}\right)$ values at different temperatures are employed, one obtains the population fractions reported in Table I.

Although the most stable conformation corresponds to the extended form of the fragment $\mathrm{C}(6)-\mathrm{O}(1)-\mathrm{C}(5)-\mathrm{C}(4)$, rotamer I is also significantly populated. The free-energy difference between the two rotamers $\left[\Delta G^{\circ}=-R T \ln \left(N_{1} / N_{\mathrm{If}}\right)\right.$ ] is only 412 $\pm 29 \mathrm{cal} / \mathrm{mol}$ at $30^{\circ} \mathrm{C}$. This energy difference is of the order of magnitude of that found by microwave spectroscopy in ethyl formate between the trans and distorted gauche rotamers ( 200 $\mathrm{cal} / \mathrm{mol}){ }^{12}$ The slightly greater value agrees with the prediction by Roberts and co-workers ${ }^{10}$ that in the acetate and formate esters of primary alcohols an increase of the size of the group attached to the $\alpha$-carbon should cause an increase in the free-energy difference between the trans and the gauche rotamers.

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## NMR of Protons Coupled to ${ }^{13} \mathrm{C}$ Nuclei Only

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In this communication we describe a simple multinuclear multipulse sequence which enables the cancellation of signals arising from protons bonded to ${ }^{12} \mathrm{C}$ nuclei, allowing the observation of just those signals of protons coupled to ${ }^{13} \mathrm{C}$. The sequence will be useful in studying ${ }^{13} \mathrm{C}$-enriched compounds obtained, for instance, in the study of biosynthetic pathways either as an alter-


Figure 1. Since precession in the rotating frame due to chemical shift is refocused at the end of the $2 \tau$ period by the $\pi[H]$ pulse, precession due only to coupling to ${ }^{13} \mathrm{C}$ is shown. (a) After a $\pi / 2[H, x]$ pulse, the magnetization vector of protons coupled to ${ }^{13} \mathrm{C}$ nuclei, which is initially along the $y$ axis of the rotating frame, splits into a clockwise rotating vector ( $H_{\mathrm{A}}$ ) and an anticlockwise rotating vector ( $H_{\mathrm{B}}$ ), corresponding to whether the ${ }^{13} \mathrm{C}$ nuclei are in the $+z$ eigenstate $\left(C_{\mathrm{A}}\right)$ or $-z$ eigenstate ( $C_{\mathrm{B}}$ ), respectively. (b) After a period $\tau=(2 J)^{-1} \mathrm{~s}, H_{\mathrm{A}}$ and $H_{\mathrm{B}}$ have precessed $90^{\circ}$ in the rotating frame. (c) A $\pi[H, y]$ pulse swaps $H_{\mathrm{A}}$ and $H_{\mathrm{B}}$. (d) After the second $\tau$ period, $H_{\mathrm{A}}$ and $H_{\mathrm{B}}$ are refocused along the $y$ axis. This refocusing is independent of any chemical shift or failure to set $\tau$ exactly. (e) If, after the first $\tau$ period [Figure 1b], $\pi[H, y], \pi[C]$ pulses are applied, $C_{\mathrm{A}}$ and $C_{\mathrm{B}}$ are also swapped, and $H_{\mathrm{A}}$ and $H_{\mathrm{B}}$ precess in directions opposite to those in Figure 1c during the second $\tau$ period. (f) After the second $\tau$ period, $H_{\mathrm{A}}$ and $H_{\mathrm{B}}$ are refocused along the $-y$ axis. This refocusing is independent of any chemical shift. Failure to set $\tau$ exactly leads to imperfect refocusing along $-y$ axis and a reduced final signal on subtraction of alternate scans.
native to or as an addition to ${ }^{13} \mathrm{C}$ NMR and in studying ${ }^{1} \mathrm{H}^{-13} \mathrm{C}$ coupling.

The simplest sequence is sequence 1 . The key to this sequence

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Figure 2. ${ }^{1} \mathrm{H}$ spectrum ${ }^{3}$ at $30^{\circ} \mathrm{C}$ of $50 \%(\mathrm{v} / \mathrm{v})$ ethylene glycol in $\mathrm{D}_{2} \mathrm{O}$ using sequence 2 , without ${ }^{13} \mathrm{C}$ decoupling during acquisition, after 500 scans. The sweep width is 200 Hz .
and sequence 2 is the judicious use of refocusing pulses. ${ }^{1}$ The $[1,0]$ for the $\pi[C]$ pulse signifies that the pulse is applied for alternate scans only. This $\pi[C]$ pulse has no effect on protons attached to molecules containing ${ }^{12} \mathrm{C}$, and signals from such protons are canceled by subtraction of alternate scans.

The mechanism of the sequence is illustrated in Figure 1. If, for example, the proton $\pi / 2$ and $\pi$ pulses are on the $x$ and $y$ axes of the rotating frame, respectively, proton magnetization of protons attached to ${ }^{12} \mathrm{C}$ nuclei, which is initially along the $y$ axis, is refocused to the $y$ axis after the second $\tau$ period, and the resulting signal is canceled by subtraction of alternate scans. For protons coupled to ${ }^{13} \mathrm{C}$ nuclei we are concerned with the magnetization vectors in Figure la: $H_{\mathrm{A}}$ and $H_{\mathrm{B}}$ comprise protons coupled to ${ }^{13} \mathrm{C}$ nuclei in the $+z$ eigenstate $\left(C_{\mathrm{A}}\right)$ and $-z$ eigenstate ( $C_{\mathrm{B}}$ ), respectively. There is no net precession of these proton vectors due to chemical shift during the $2 \tau$ period as this is refocused by the $\pi[H]$ pulse as before. Indeed, for scans in which no $\pi[C]$ pulse is applied, precession due to coupling to ${ }^{13} \mathrm{C}$ is also refocused as illustrated in Figure 1a-d. However, the direction of this precession is reversed by the application of a $\pi[C]$ pulse as shown in Figure 1e, and the proton magnetization is refocused along the $-y$ axis at the end of the second $\tau$ period, as in Figure 1f, if $\tau=$ $(2 J)^{-1}$ where $J$ is the ${ }^{1} \mathrm{H}^{13} \mathrm{C}$ coupling constant. Thus alternate application of the $\pi[C]$ pulse and subtraction of alternate scans will cause summation of signals arising from $H_{\mathrm{A}}$ and $H_{\mathrm{B}}$.
Sequence 1 should be quite successful with modern recent spectrometers employing stable, superconducting magnets. Our system, an iron-core electromagnet, suffers sufficiently from drift in the deuterium lock signal that it is not possible to cancel signals by subtraction of alternate scans to better than $2 \%$. Although this degree of cancellation of signals of protons attached to ${ }^{12} \mathrm{C}$ nuclei is probably sufficient for the study of ${ }^{13} \mathrm{C}$-enriched samples, it is desirable to improve upon it. To this end sequence 2 was devised. If, for example, the first $\pi[H]$ pulse is on the $y$ axis,

the first $\pi[H], \pi[C]$ pulse ensures that the $H_{\mathrm{A}}$ and $H_{\mathrm{B}}$ vectors are along the $-x$ and $x$ axes at the end of the first $\tau$ period [if $\tau=$ $\left.(2 J)^{-1}\right]$ but that proton magnetizations of protons attached to ${ }^{12} \mathrm{C}$ are along the $y$ axis. Thus the $\pi / 2[-x]$ pulse has no effect on $H_{\mathrm{A}}$ and $H_{\mathrm{B}}$ but returns the unwanted proton magnetization to the $z$ axis. Pulsing about the $-x$ axis reduces the effect of imperfections and inhomogeneities in the initial $\pi / 2[x]$ pulse. $H_{\mathrm{A}}$ and $H_{\mathrm{B}}$ are refocused along the $y$ or $-y$ axes after the second $\tau$ period, depending on the alternate application of the $\pi[C]$ pulse between the two $\tau$ periods. This enables subtraction of alternate scans as in sequence 1 so that residual unwanted signals, resulting from imperfections in the pulses and relaxation during the first $\tau$ period, are canceled.


Figure 3. ${ }^{1} \mathrm{H}$ spectra ${ }^{3}$ at $30^{\circ} \mathrm{C}$ of pure (external D lock) 1-methylnorbornane, approximately $60 \%{ }^{13} \mathrm{C}$-enriched at the methyl group. The sweep width is 250 Hz . Sixty-four scans were collected. (a) Normal spectrum, (b) using sequence 2 without ${ }^{13} \mathrm{C}$ decoupling during acquisition, and (c) using sequence 2 with ${ }^{13} \mathrm{C}$ decoupling during acquisition.

As illustrated in Figure 2 for ethylene glycol, sequence 2 enables cancellation of the unwanted signals to better than $0.2 \%$ even for our imperfect magnet. (The ${ }^{13} \mathrm{C}$ satellites are split by homonuclear coupling unlike the central resonance and thus have a normal amplitude of about $0.1 \%$ of the central line.) Integration across the center line is considerably less than $0.2 \%$ of the uncanceled signal.

The application of the sequence to an enriched sample is shown in Figure 3. Although the ${ }^{13} \mathrm{C}$ satellites are clearly resolved in Figure 3a, the ${ }^{12} \mathrm{CH}$-canceled spectrum [Figure 3b and the decoupled ${ }^{12} \mathrm{CH}$-canceled spectrum (Figure 3c)] clearly illustrate what can be achieved for enriched samples where the ${ }^{13} \mathrm{C}$ satellites are normally overlapped by other resonances.
${ }^{13} \mathrm{C}$-enriched quaternary carbons can be studied by setting $\tau$ to approximately correspond to a long-range $J$ value. Indeed, use of larger $\tau$ values provides a general method of studying long-range ${ }^{13} \mathrm{C}-{ }^{1} \mathrm{H}$ coupling in enriched compounds if ${ }^{13} \mathrm{C}$ decoupling is not employed during acquisition. However, the greatest potential use of these sequences is in studying both short- and long-range ${ }^{13} \mathrm{C}-{ }^{1} \mathrm{H}$ coupling by two-dimensional NMR of unenriched compounds. Incrementation of $\tau$ to provide a second $J$ dimension and ${ }^{13} \mathrm{C}$ decoupling during acquisition will produce a resonance in the $J$ dimension for each ${ }^{13} \mathrm{C}^{-1} \mathrm{H}$ coupling at $J / 2 \mathrm{~Hz}$. Although these peaks will be split by proton homonuclear coupling, there will be a large gain in sensitivity over ${ }^{13} \mathrm{C}$ two-dimensional $J$ spectra, ${ }^{2}$ and the problem of complicated ${ }^{13} \mathrm{C}-{ }^{1} \mathrm{H}$ coupled multiplets is avoided. Since the proton homonuclear coupling occurs in both dimensions, it will assist in resolution.

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## A New Approach to the Conformational Analysis of Seven-Membered Rings

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Progress in the conformational analysis of seven-membered rings has been slow, chiefly because pseudorotation of these rings is facile. ${ }^{1,2}$ Evidence about the nature of the conformational energy surfaces for such systems and about such factors as axial-equatorial energy differences has come mainly from force-field calculations, with experimental support ${ }^{1,3}$ for the nature of the lowest minima. Considerable advances were made in the conformational analysis of six-membered rings through the examination of the properties of derivatives with one or sometimes two groups present to lock the ring in a particular conformation., ${ }^{4,5}$ We show here that the introduction of three groups results in comparable simplification of the conformational situation for seven-membered rings. We illustrate the procedure by using $2,4,7$-trisubstituted-1,3-dioxepanes because these compounds are easily synthesized ${ }^{6}$ and equilibrated.

For cycloheptane, there are 14 degenerate lowest energy conformations, the twist-chairs (TC), which pseudorotate into each other through 14 degenerate maxima, the chairs (calculated barrier, ${ }^{1} 1.3 \mathrm{kcal} \mathrm{mol}^{-1}$ ). Fourteen boat (B) and twist-boat (TB) conformations (calculated stabilities ${ }^{1}$ relative to the TC, 3.42 and $3.39 \mathrm{kcal} \mathrm{mol}^{-1}$, respectively) also pseudorotate into each other and are accessible from the TC conformation via an inversion process (barrier ${ }^{1} 9.7 \mathrm{kcal} \mathrm{mol}^{-1}$ ). For 1,3 -dioxepane, there are four types of TC conformations, A-D, shown with their calculated stabilities. ${ }^{1}$ Chair conformations are again local maxima so they will not be considered further here.

2.55

2.55

2.65

$0.0 \mathrm{Kcal}^{-\mathrm{mol}^{-1}}$

Three stereoisomers (1,2, and 3) are produced when three


2

3

substituents are introduced at positions 2, 4, and 7 of 1,3 -dioxepane, if those at 4 and 7 are identical. The relative energies of the TC conformations of the three stereoisomers with all groups methyl (1a, 2a, 3a) were evaluated approximately by making the following assumptions: (1) The four types of 1,3-dioxepane TC conformations have the energies calculated by Bocian and Strauss. ${ }^{1}$ (2) The introduction of a methyl group at a particular position in a conformation increases the energy of the conformation by the amount calculated ${ }^{2}$ for a similar introduction for cycloheptane. This $A$ value is decreased by one-quarter of its value whenever

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